

Course Syllabus

ISYE OMSA-6644

Simulation and Modeling for Engineering and Science

Fall 2025

(revised 7/30/25)

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Course Description

This course covers modeling of discrete-event dynamic systems and introduces simulation-based methods for using these models to solve engineering design and analysis problems.

Prerequisites

You will be expected to come in knowing a bit of basic calculus, probability, and statistics. But don't worry too much – we'll provide bootcamps on that material so as to make the class pretty much self-contained. In addition, this course will involve extensive computer programming, so it would be nice to have at least a little experience in something like Excel, just to bring back the programming memories.

Course Goals

- Learn how to develop simulation models and conduct simulation studies.
- Become familiar with the organization of simulation languages. In particular, we will do a great deal of modeling with Arena, a comprehensive simulation package with animation capabilities.
- Review statistical aspects including input analysis, random variate generation, output analysis, and variance reduction techniques.

Syllabus

- We make occasional changes to this wonderful syllabus.
- All nontrivial changes will be announced on Canvas.
- You are responsible for keeping up with any changes.

Grading Policies

- There will be two **midterms** and a **final exam**. Test questions are typically multiple choice or T/F.
- There will be 13 **Homework** assignments (not as bad as it sounds). There will be a bunch of bonus questions spread throughout the semester, which you can do to earn a few extra points. **HWs that are late will suffer a 10x% deduction, where x is the number of days late, with x = 3 being the upper bound on the allowed lateness.** So plan ahead!

- We will have a **project**, which you can select from among several theory- and applications-oriented topics. You will be allowed to work in small groups.
- **Turn Stuff in On-time!** Whether it's HWs, projects, or tests, **please** get things to us when you're supposed to. We give you very long windows and lots of warning, so you have plenty of time to plan ahead. Because our class is so large, *it will be very, very difficult to accommodate you if you miss a deadline.*
- You must achieve an overall weighted average of 60% to pass the course.
- Work hard and you will be rewarded – Grading is usually pretty generous. 😊
- Grading Disputes:
 - **Let's be winners, not whiners.** We are happy to discuss grades, but please make reasonable requests. 😊
 - To this end, we will generously provide various **bonus point opportunities** throughout the course; but because of this lovely act of kindness, we will not accept any test grade whining for matters involving up to 4 points. (Makes great sense, eh?!)

Mother Teresa: "Wow, that's something nice that I would do!"
 - If you really, really want to request a regrade (for matters involving more than 4 points), simply fill out the convenient form that can be found at <http://www.isye.gatech.edu/%7Esman/courses/gradegrovel.pdf>.

- Grading Breakdown

Homework	10%
Project	10%
Midterm Exam 1	25%
Midterm Exam 2	25%
Final Exam	30%
Bonus Opportunities	2.5%
TOTAL	102.5%

Homework, Project, and Exam Due Dates

All homeworks, projects, and tests will be due at the times in the table at the end of this syllabus. These times are subject to change so please check back often. Please convert from Eastern Time (EDST/EST, Atlanta) to your local time zone using a [Time Zone Converter](#).

Timing Policy

- The Modules follow a logical sequence, so they (mostly) need to be done in order.
- Homework Assignments and the Project should be completed by their due dates.
- Quizzes must be completed during the time allotted on the schedule.
- You will have access to the course content for the scheduled duration of the course.

Exam Policy

- For Quiz x ($x = 1, 2, 3$), you are allowed to use x sheets of paper, either 8.5"x11" or A4, with handwritten or printed notes (both sides of the sheet, 2x sides total).
- For all quizzes, you are allowed a blank sheet of paper for scratch work. (All OMS Analytics and OMS CS students will be proctored by Honorlock; you will have to show the front and back of the blank sheet while you are being proctored.)
- You are also allowed to bring any reasonable calculator.
- You will **not** be allowed to use packages such as Excel, Arena, R, etc. during the exams.

Attendance Policy

- This is a fully online course.
- Login on a regular basis to complete your work, so that you do not have to spend a lot of time reviewing and refreshing yourself regarding the content.

Plagiarism Policy

- Plagiarism is considered a serious offense. You are not allowed to copy and paste or submit materials created or published by others, as if you created the materials. All materials submitted and posted must be your own.
- These days, there is a lot of buzz regarding ChatGPT (and related applications). We suppose that you can use ChatGPT to help you with very preliminary versions of some of your written verbiage, but (i) *do not let ChatGPT do your thinking for you*, and (ii) *make sure to properly and thoroughly cite your use of ChatGPT*.

Student Honor Code

All GT students should abide by the Georgia Tech Student Honor Code.

- Review the Georgia Tech Student Honor Code:
<https://osi.gatech.edu/content/honor-code>
- You are responsible for completing your own work.
- Any GT student suspected of behavior in violation of the Georgia Tech Honor Code will be referred to Georgia Tech's Office of Student Integrity.

Communication

- Feel totally free to contact your instructor, teaching assistants, and fellow learners via the **Piazza** discussion forums. Our Piazza access code is **f24_isye6644**. (*Please, please, please do not email the instructor directly unless it's something really, really important.*) Often, discussions with fellow learners are the sources of key pieces of learning and are often funny and entertaining. Some suggestions:
 - Always be courteous and nice (see Netiquette below).
 - Please make sure that your subject line **PRECISELY** states what problem you are asking about, as failure to do so causes everyone a great deal of time trying to figure out what you need. For instance, "Fall 2023 Practice Test 3, Question 5a".
 - Your problem may have already been addressed! So make sure that you sniff around the Piazza forum to see if that's the case! That avoids repetitive and redundant and repetitive repetition.
 - Think about your problem a bit and give it the old college try before asking about it on Piazza. Don't give up too early before you punt!

Netiquette

- Netiquette refers to etiquette that is used when communicating on the Internet. Review the Core Rules of Netiquette. When you are communicating via email, discussion forums or synchronously (in real-time), please use correct spelling, punctuation, and grammar consistent with the academic environment and scholarship¹.
- We expect all course participants (learners, faculty, teaching assistants, staff) to interact respectfully. *You must always play nice with your fellow students and dedicated TAs.* Learners who do not adhere to this guideline may be removed from the course.

¹Conner, P. (2006–2014). Ground Rules for Online Discussions, Retrieved 8/14/2020 from <https://tilt.colostate.edu/TipsAndGuides/Tip/128>

Course Materials

- All content and course materials can be accessed online.
- There is no required textbook for this course, though students are encouraged to find copies of the following references:
 - Law, A. M., *Simulation Modeling and Analysis*, 5th edition, McGraw-Hill Education, New York, 2015. [This textbook is most for the “theory” aspects of the course.]
 - Kelton, W. D., Zupick, N. B., and Ivey, N., [*Simulation with Arena*, 7th edition](#), McGraw-Hill, New York, 2024. [This book covers the Arena simulation language.]
 - If you want to review probability and statistics, you go to my ISYE 6739 course website www.isye.gatech.edu/~sman/courses/6739 for complete course materials; and/or you can (i) get a **free** copy of my wonderful book, *A First Course in Probability and Statistics*, from our ISYE 6644 Canvas site, or (ii) buy an **el cheapo softbound version here** (just click). We’ve heard that this makes a frightfully wonderful Halloween gift for the whole family!



Technology/Software Requirements

- Internet connection (DSL, LAN, or cable connection desirable)
- R statistical software (free download; see cran.r-project.org)
- Arena simulation software
 - Arena is **free!** Get it [here](#) (but make sure to click the “Student” option on the “Job Type” menu)!
 - *Arena requires a Windows operating system* to run on your computer.
 - If you don’t have Windows, you can run Arena thru ISyE’s Virtual Lab. To get an account, see <https://www.isye.gatech.edu/academics/doctoral/current-students/computing#services>
 - Arena (and our corresponding lecture material) is currently transitioning to a new version, so the latest Arena version doesn’t perfectly match what’s in the notes. The good news is that everything still works. 😊
- Adobe Acrobat PDF reader (free download; see <https://get.adobe.com/reader/>)

Disabilities and Special Circumstances

- If you have an issue requiring special accommodations, please make an appointment with the Office of Disability Services to discuss the appropriate procedures. Their website is <http://disabilityservices.gatech.edu>
- In some cases, religious observances or other events may conflict with scheduled class activities. *In such situations students can be given an alternative means of meeting the academic requirement.* **Students must notify the instructor of any such conflicts, with the specific dates, within the first two weeks of classes.** Students requiring disability accommodations are also requested to make arrangements with the instructor, within the same period if possible.
- We will work with you if you come down with any significant illness. Potential solutions include granting small time extensions, re-weighting test scores if you happen to miss one, and even giving an incomplete (as a last resort).

Course Topics and Pacing Schedule

The table below contains a course topic outline and homework due dates. [Note that some topics below are marked as **OPTIONAL**. You will not be given mandatory homework nor will you be tested on those topics; but we have nevertheless included this material in case you need additional review or would like to delve into a topic further.]


Weeks	Course Topics	Release Dates (all times EDT/EDST)
Week 1 (Aug 18–22)	Module 1: Whirlwind Tour of Simulation Lesson 1: Getting to Know You Lesson 2: Syllabus Lesson 3: Whirlwind Tour Lesson 4: Whirlwind Tour – History Lesson 5: What Can We Do for You Lesson 6: Some Baby Examples Lesson 7: More Baby Examples Lesson 8: Generating Randomness Lesson 9 [OPTIONAL] : Simulation Output Analysis	M Aug 18 at 8:00 a.m.
Week 1 Homework	Homework 1	F Aug 22 at 8:00 a.m. – F Aug 29 at 11:59 p.m.
Week 2 (Aug 25–29)	Module 2: Bootcamps Lesson 1 [OPTIONAL] : Calculus Primer Lesson 2 [OPTIONAL] : Saved By Zero! Solving Equations Lesson 3 [OPTIONAL] : Integration Lesson 4 [OPTIONAL] : Integration Computer Exercises Lesson 5: Probability Basics Lesson 6: Simulating Random Variables Lesson 7: Great Expectations Lesson 8: Functions of a Random Variable Lesson 9: Jointly Distributed Random Variables	M Aug 25 at 8:00 a.m.
Week 2 Homework	Homework 2	F Aug 29 at 8:00 a.m. – F Sept 5 at 11:59 p.m.
Week 3 (Sept 1–5) Labor Day Sept 1	Module 2 (cont): Some More Bootcamps Lesson 10 [OPTIONAL] : Conditional Expectation Lesson 11: Covariance and Correlation Lesson 12: Probability Distributions Lesson 13: Limit Theorems Lesson 14 [OPTIONAL] : Introduction to Estimation Lesson 15 [OPTIONAL] : Maximum Likelihood Estimation	M Sept 1 at 8:00 a.m.

	Lesson 16 [OPTIONAL] : Confidence Intervals	
Week 3 Homework	Homework 3	F Sept 5 at 8:00 a.m. – F Sept 12 at 11:59 p.m.
Week 4 (Sept 8–12)	Module 3: Hand Simulations Lesson 1: Stepping Through Differential Equation Lesson 2: Monte Carlo Integration Lesson 3: Monte Carlo Integration Demo Lesson 4: Making Some Pi Lesson 5: A Single-Server Queue Lesson 6: An (s,S) Inventory System Lesson 7: An (s,S) Inventory System Demo Lesson 8: Simulating Random Variables Lesson 9: Simulating Random Variables Demo Lesson 10: Spreadsheet Simulation	M Sept 8 at 8:00 a.m.
Week 4 Homework	Homework 4	F Sept 12 at 8:00 a.m. – F Sept 19 at 11:59 p.m.
Week 5 (Sept 15–19)	Module 4: General Simulation Principles Lesson 1: Steps in a Simulation Study Lesson 2: Some Useful Definitions Lesson 3: Time-Advance Mechanisms Lesson 4: Two Modeling Approaches Lesson 5: Simulation Languages	M Sept 15 at 8:00 a.m.
Project Milestone 1	Project Topics Announced	M Sept 15 at 8:00 a.m. Topic and group selection due F Sept 26 at 11:59 p.m.
Week 5 Homework	Homework 5	F Sept 19 at 8:00 a.m. – F Sept 26 at 11:59 p.m.
Week 6 (Sept 22–26)	Module 5: The Arena Simulation Language Lesson 1: Introduction Lesson 2: Process-interaction Lesson 3: Let's Meet Arena! Lesson 4: The Arena Basic Template Lesson 5: Create-Process-Dispose Modules Lesson 6: The Process Module	M Sept 22 at 8:00 a.m.

	<p>Lesson 7: Resource, Schedule, and Queue Spreadsheets</p> <p>Lesson 8: The Decide Module</p> <p>Lesson 9: The Assign Module</p> <p>Lesson 10: Attribute, Variable, and Entity Spreadsheets</p> <p>Lesson 11: Arena Internal Variables</p> <p>Lesson 12: Displaying Stuff</p> <p>Lesson 13: Batch, Separate, and Control</p> <p>Lesson 14: Run Setup and Control</p>	
Week 6 Homework	Homework 6	F Sept 26 at 8:00 a.m. – F Oct 3 at 11:59 p.m.
Midterm Exam 1	Midterm Exam 1 [Covers everything up to and including Lesson 9 from Week 6. See Topics Attachment.]	F Sept 26 at 8:00 a.m. – Su Oct 5 at 11:59 p.m.
Week 7 (Sept 29–Oct 3)	<p>Module 5 (cont.): More Arena</p> <p>Lesson 15: Two-Channel Manufacturing Example</p> <p>Lesson 16: Fake Customers</p> <p>Lesson 17: The Advanced Process Template</p> <p>Lesson 18: Resource Failures + Maintenance</p> <p>Lesson 19: The Blocks Template</p> <p>Lesson 20: The Joy of Sets</p> <p>Lesson 21: Description of Call Center</p> <p>Lesson 22: Call Center Demo</p> <p>Lesson 23: An Inventory Model</p> <p>Lesson 24: One Line vs Two Lines?</p> <p>Lesson 25: A Re-entrant Queue</p> <p>Lesson 26: SMARTS Files and Rockwell Demos</p> <p>Lesson 27: A Manufacturing System Demo</p>	M Sept 29 at 8:00 a.m.
Week 7 Homework	Homework 7	F Oct 3 at 8:00 a.m. – F Oct 10 at 11:59 p.m.
Week 8 (Oct 6–10) Fall Break (Oct 6, 7)	<p>Module 5 (cont.): Still More Arena</p> <p><i><u>The following lessons are NOT OPTIONAL (in spite of what the videos may say)!</u></i></p> <p>Lesson 28: Mfg System Details: Advanced Transfer Panel</p> <p>Lesson 29: Mfg System Details: Sequences</p> <p>Lesson 30: Mfg System Details: Advanced Sets</p> <p>Lesson 31: Mfg System Details: Model Walk-Through</p> <p>Lesson 32: Mfg System Details: Transporters and Conveyors</p> <p>Module 6: Random Number Generation</p> <p>Lesson 1: Introduction</p>	M Oct 6 at 8:00 a.m.

	<p>Lesson 2: Some Lousy Generators</p> <p>Lesson 3: Linear Congruential Generators</p> <p>Lesson 4: Tausworthe Generators</p> <p>Lesson 5: Generalization of LCGs</p> <p>Lesson 6: Choosing a Good Generator – Some Theory</p> <p>Lesson 7: Choosing a Good Generator – Statistics Tests, Intro</p> <p>Lesson 8: Choosing a Good Generator – Goodness-of-Fit Tests</p> <p>Lesson 9: Choosing a Good Generator – Independence Tests I</p> <p>Lesson 10: [OPTIONAL]: Independence Tests II</p>	
Week 8 Homework	Homework 8	F Oct 10 at 8:00 a.m. – F Oct 17 at 11:59 p.m.
Week 9 (Oct 13–17)	<p>Module 7: Random Variate Generation</p> <p>Lesson 1: Introduction</p> <p>Lesson 2: Inverse Transform Method</p> <p>Lesson 3.1: ITM – Continuous Examples</p> <p>Lesson 3.2: ITM – Continuous Examples DEMO 1</p> <p>Lesson 3.3: ITM – Continuous Examples DEMO 2</p> <p>Lesson 4: Inverse Transform Method - Discrete Examples</p> <p>Lesson 5 [OPTIONAL]: ITM – Empirical Distributions</p> <p>Lesson 6.1: Convolution Method</p> <p>Lesson 6.2: Convolution Method DEMO</p> <p>Lesson 7: Acceptance-Rejection Method</p> <p>Lesson 8 [OPTIONAL]: Proof of the A-R Method</p> <p>Lesson 9.1: A-R Method – Continuous Examples</p> <p>Lesson 9.2: A-R Method – Continuous Examples DEMO</p> <p>Lesson 10: A-R Method – Poisson Distribution</p>	M Oct 13 at 8:00 a.m.
Project Milestone 2	Project Progress Report (nice and simple; rubric TBA)	Due F Oct 17 at 11:59 p.m.
Week 9	Homework 9	F Oct 17 at 8:00 a.m. – F Oct 24 at 11:59 p.m.
Week 10 (Oct 20–24)	<p>Module 7 (cont.): More RV Generation</p> <p>Lesson 11: Composition</p> <p>Lesson 12: Box-Muller Normal RVs</p> <p>Lesson 13: Order Statistics Other Stuff</p> <p>Lesson 14: Multivariate Normal Distribution</p> <p>Lesson 15: Baby Stochastic Processes</p> <p>Lesson 16.1: Nonhomogeneous Poisson Processes</p> <p>Lesson 16.2: Nonhomogeneous Poisson Processes DEMO</p> <p>Lesson 17.1: Time Series</p> <p>Lesson 17.2: Time Series DEMO</p> <p>Lesson 18: Queueing</p>	M Oct 20 at 8:00 a.m.

	Lesson 19.1: Brownian Motion Lesson 19.2: Brownian Motion DEMO	
Week 10 Homework	Homework 10	F Oct 24 at 8:00 a.m. – F Oct 31 at 11:59 p.m.
Midterm Exam 2	Midterm Exam 2 [Covers everything up to and including Lesson 13 from Week 10, with emphasis on more-recent stuff. See Topics Attachment.]	F Oct 24 at 8:00 a.m. – Su Nov 2 at 11:59 p.m.
Week 11 (Oct 27–31)	Module 8: Input Analysis Lesson 1: Introduction Lesson 2: Identifying Distributions Lesson 3: Unbiased Point Estimation Lesson 4: Mean Squared Error Lesson 5: Maximum Likelihood Estimators Lesson 6: MLE Examples Lesson 7: Invariance Property of MLEs Lesson 8 [OPTIONAL] : The Method of Moments Lesson 9: Goodness-of-Fit Tests Lesson 10: Exponential Example Lesson 11: Weibull Example Lesson 12: Still More Goodness-of-Fit Tests Lesson 13: Problem Children Lesson 14: Demo Time	M Oct 27 at 8:00 a.m.
Week 11 Homework	Homework 11	F Oct 31 at 8:00 a.m. – F Nov 7 at 11:59 p.m.
Week 12 (Nov 3–7)	Module 9: Output Analysis Lesson 1: Introduction Lesson 2: Mathematical Interlude [Don't Panic!] Lesson 3: Finite-Horizon Analysis Lesson 4: Finite-Horizon Extensions Lesson 5: Simulation Initialization Issues Lesson 6: Steady-State Analysis Lesson 7: Properties of Batch Means Lesson 8: Other Steady-State Methods	M Nov 3 at 8:00 a.m.
Week 12 Homework	Homework 12	F Nov 7 at 8:00 a.m. – F Nov 14 at 11:59 p.m.
Week 13 (Nov 10–14)	Module 10: Comparing Systems Lesson 1: Introduction	M Nov 10 at 8:00 a.m.

	<p>Lesson 2: Confidence Interval for the Mean</p> <p>Lesson 3: CIs for the Difference in Two Means</p> <p>Lesson 4: Paired CI for the Difference in Two Means</p> <p>Lesson 5: CIs for the Mean Difference in Simulations</p> <p>Lesson 6: Common Random Numbers</p> <p>Lesson 7: Antithetic Random Numbers</p> <p>Lesson 8 [OPTIONAL]: Control Variates</p> <p>Lesson 9: Ranking and Selection Methods</p>	
Week 13 Homework	Homework 13	F Nov 14 at 8:00 a.m. – F Nov 21 at 11:59 p.m.
Weeks 14 + 15 (Nov 17–Dec 2) Thanksgiving Break (Nov 26–28) 	Module 10 (cont.): More Comparing Systems Lesson 10: Normal Means Selection Lesson 11: Single-Stage Normal Means Procedure Lesson 12: Normal Means Extensions Lesson 13: Bernoulli Probability Selection Lesson 14: Bernoulli Extensions Lesson 15: Multinomial Cell Selection Lesson 16: Multinomial Procedure + Extensions Lesson 17: Summary	M Nov 17 at 8:00 a.m.
Project Milestone 3	Project Due	Due Tu Dec 2 at 11:59 p.m.
Final Exam	Final Exam [Covers everything, with emphasis on more-recent stuff. See Topics Attachment below.]	Tu Dec 2 at 8:00 a.m. – W Dec 10 at 11:59 p.m.

Test Topix for ISyE 6644, Fall 2024

- I've tried my best to make this list as complete as possible, but I may have missed a topic or two. That being said, you are responsible for everything that we do in class or homework.
- As GT students, you are expected to formulate problems and solution strategies which are more than mere rote regurgitation of material you learned in class. Thus, you shouldn't be surprised if some questions cover natural extensions of material from class.
- I'll supply all necessary tables, e.g., $N(0,1)$, t , and χ^2 , but you can feel free to use your own.

TEST 1 TOPIX

1. Intro Material

- a. Definition of simulation
- b. Advantages and disadvantages of simulation
- c. History of simulation
- d. Typical questions and applications

2. Calculus, Probability, and Statistics Review

- a. **Calculus [not really responsible for this material, except I might make you search for a zero]**
 - i. Basic definitions
 - ii. Derivatives
 - iii. Solving for zeros
 - iv. Integration
 - v. Numerical integration
- b. Probability Preliminaries
 - i. Conditional probability
 - ii. Independent events
 - iii. Definition of random variable
 - iv. Discrete RV's and probability mass function
 - v. Continuous RV's and probability density function
 - vi. Cumulative distribution function
- c. Simulating RV's (first pass)
 - i. Discrete uniform distribution
 - ii. General discrete distribution
 - iii. Inverse Transform Theorem for continuous RV's
 - iv. Exponential (and other) continuous distributions via IVT.
 - v. Generating $U(0,1)$'s via desert island algorithm, including walk-through of pseudo-code.

- d. Expected Values
 - i. Definition
 - ii. Discrete and continuous examples of expected value
 - iii. Law of the Unconscious Statistician
 - iv. Moments, central moments, variance, standard deviation
 - v. Discrete and continuous examples of LOTUS
 - vi. Moment generating function
 - vii. Examples and properties of mgf's
- e. Functions of a RV
 - i. Discrete examples
 - ii. Continuous examples
 - iii. IVT methods (again) with examples
 - iv. Relationship with LOTUS
- f. Jointly distributed RV's
 - i. Definition of joint cdf
 - ii. Marginal cdf's
 - iii. Joint and marginal pmf's
 - iv. Joint and marginal pdf's
 - v. Examples for discrete and continuous cases
 - vi. Independent RV's
 - vii. Conditional pmf's and pdf's
 - viii. **Conditional expectation [this won't be on the test]**
 - ix. **Double expectation $E(E(Y|X)) = EY$, including examples [this won't be on the test]**
- g. Covariance and correlation
 - i. Definitions
 - ii. Relationship between independence and correlation
 - iii. Examples
 - iv. Miscellaneous properties (e.g., $\text{Var}(X+Y)$, bounds on correlation, etc.)
- h. Probability distributions
 - i. Discrete distributions
 - 1. Bernoulli
 - 2. Binomial
 - 3. Geometric
 - 4. Poisson (including discussion on Poisson processes)
 - ii. Continuous distributions
 - 1. Uniform
 - 2. Exponential (including memoryless property)
 - 3. Erlang, Gamma distributions
 - 4. Triangular
 - 5. Normal (including Standard Normal)

- 6. Other sampling distributions (including chi-square, t, F, and various relationships with each other)
- i. Limit theorems
 - i. Linear combinations of independent normal (including distribution of sample mean)
 - ii. Convergence in distribution
 - iii. Law of Large Numbers
 - iv. Central Limit Theorem for independent and identically distributed data.
 - v. Examples
- j. Statistics Tidbits **[this material will eventually be covered in modules 8, 9, 10, so it's in fair territory to have it on the final! 😊]**
 - i. Properties of sample mean and sample variance
 - ii. Confidence intervals for the mean and variance

3. Hand Simulations

- a. "Simulating" a differential equation
- b. Monte Carlo integration
- c. Determining π via simulation (dart tossing on a circle and sphere)
- d. Single-server queue (including FIFO and LIFO service disciplines)
- e. (s,S) inventory system
- f. Simulating RV's (repeats some material from the Prob/Stats review)
- g. Spreadsheet simulation (e.g., stock portfolio in Excel)

4. General Simulation Principles

- a. Steps in a simulation study
- b. List of various simulation definitions (e.g., event, system state, simulation clock, etc.)
- c. Event-Scheduling vs. Process Interaction modeling approaches
- d. How are events processed?
- e. Future events list + extended example
- f. Simulation languages – what to look for

Plus, the first few Arena mini-topix below...

5. Arena

- a. Layout of Arena screen (panels, modules, etc.)
- b. Basic Process template: CREATE-PROCESS-DISPOSE modules
- c. SEIZE-DELAY-RELEASE inside of the PROCESS module.
- d. Resource, Schedule, Queue, Entity, and other spreadsheets
- e. DECIDE module – probabilistic and conditional routing
- f. ASSIGN module

TEST 2 TOPIX

Everything from Test 1 + the following (with less emphasis placed on the Test 1 material)...

- g. Simple examples, e.g. (partial list),
 - i. Single-server queue
 - ii. Parallel servers
 - iii. Schedules for servers
 - iv. Multiple arrival streams
- h. Displays, graphics, etc.
- i. BATCH and SEPARATE modules
- j. Run set-up and control
- k. More-sophisticated queueing networks (e.g., two-channel manufacturing example, call center example)
 - i. Advanced Process modules (e.g., SEIZE, DELAY, RELEASE modules)
 - ii. Some primitive blocks (e.g., QUEUE)
 - iii. Use of “pretend” customers
 - iv. Nonhomogeneous Poisson arrivals
 - v. Use of resource sets, including how to prioritize servers
 - vi. Use of submodels
- l. Inventory processes
- m. Crazy examples such as re-entrant queues
- n. SMARTS files and other Rockwell examples
- o. Manufacturing systems
 - i. Advanced Transfer modules (e.g., ROUTE, ENTER, LEAVE)
 - ii. Sequences of customer visitation locations
 - iii. Advanced sets of sequences
 - iv. Transporters and conveyors

6. Uniform Random Number Generation

- a. Overview – desirable properties of a pseudo-random number generator
- b. Some generators we won't use, e.g.,
 - i. PRN's from tables
 - ii. Midsquare
- c. Linear congruential generators
 - i. Cycling
 - ii. 16807 desert island generator (again)
 - iii. RANDU (a bad generator)
- d. Tausworthe generator
- e. Combined generators
 - i. L'Ecuyer's generator of cycle length 2^{191}

- ii. Mersenne Twister
- f. Some theoretical considerations, e.g., from Knuth's book
- g. Statistical tests for randomness
 - i. Goodness-of-fit test – Chi-squared
 - ii. Runs tests for independence
 - 1. Runs up and down
 - 2. Runs above and below the mean
 - 3. **Autocorrelation test [this won't be on the test]**

7. Random Variate Generation

- a. Inverse Transform Theorem (yet again)
 - i. Proof
 - ii. Discrete example adaptations
 - iii. Continuous examples
 - 1. Easy ones such as Exponential, Weibull, etc.
 - 2. Slightly harder examples such as Triangle distribution
 - 3. Normal distribution, both exact and approximate methods
 - iv. Special case methods, e.g., Geometric
 - v. **Empirical distributions [this won't be on the test]**
- b. Convolution method
 - i. Binomial
 - ii. Triangle
 - iii. Erlang
 - iv. CLT
 - 1. Desert island sum of Uniforms to generate Normal
 - 2. Normal approximation to Poisson (including continuity correction)
 - v. Cauchy
 - 1. Cauchy's add up to another Cauchy
 - 2. IVT method
 - 3. Ratio of two Normals
- c. Acceptance-Rejection methods
 - i. Trivial Uniform example
 - ii. Some discussion on general method
 - iii. **Proof of the general method [don't expect to see this on the test, unless I'm in a really bad mood!]**
 - iv. Examples involving polynomial and half-normal p.d.f.'s
 - v. Poisson distribution
- d. Composition
- e. Special-case techniques
 - i. Box-Muller method for Normal distribution
 - ii. Extensions of B-M, e.g., Cauchy, Chi-squared.

- iii. Generating min's and max's of iid RV's, e.g., min of iid Exponentials.

TEST 3 (FINAL) TOPIX

Everything in the freaking course, including the following new stuff (with less emphasis placed on the Tests 1 and 2 material)...

- f. Multivariate Normal
 - i. Definition in 2 and then >2 dimensions
 - ii. Cholesky decomposition method for generating realizations (exact expression in 2 dimensions, algorithm for >2 dimensions)
- g. Stochastic processes
 - i. Markov chains
 - ii. Poisson processes
 - iii. Nonhomogeneous Poisson processes (via thinning method)
 - iv. Time series
 - 1. MA(1)
 - 2. AR(1)
 - 3. EAR(1)
 - 4. ARTOP
 - v. M/M/1 queue waiting times
 - vi. Brownian motion
 - 1. Definition and history
 - 2. Elementary properties, including covariance structure
 - 3. General CLT
 - 4. How to generate
 - 5. Geometric BM and financial applications

8. Input Analysis

- a. General discussion
 - i. Careful about GIGO with respect to simulation input
 - ii. What makes a good distribution
 - iii. Identification of obvious distributions
- b. Estimation review
 - i. Unbiased estimators
 - 1. Definition
 - 2. Sample mean
 - 3. Sample variance
 - 4. Other examples such as $\text{Unif}(0,\theta)$
 - ii. Mean squared error

- iii. Maximum likelihood estimators
 - 1. Definition
 - 2. Examples such as Exponential
 - 3. Two-dimensional examples such as Normal with unknown mean and variance
 - 4. Other tougher examples such as $\text{Unif}(0, \theta)$ and Gamma
 - 5. Invariance Property + examples
 - iv. **Method of Moments [this won't be on the test (sorry, MoM!)]**
- c. Goodness-of-fit tests for input distributions
 - i. Chi-squared for Exponential
 - ii. Chi-squared for Weibull, including search techniques such as bisection and Newton
 - iii. Kolmogorov-Smirnov
 - iv. More goodness-of-fit tests
- d. Problem Children
 - i. Little or no data
 - ii. Data from an unusual distribution
 - iii. Nonstationary data
 - iv. Multivariate / correlated data
- e. Arena Input Analyzer demo

9. Output Analysis

- a. Introduction
 - i. The need for output analysis in a proper statistical study
 - ii. Simulation data isn't iid normal, and this is a problem
 - iii. Types of output analysis – finite-horizon (terminating) and steady-state
- b. A mathematical interlude related to the fact that the variance of the sample mean isn't $\text{Var}(X_i)/n$, and its consequences **[I might ask you to calculate the variance of the sample mean for a specific process, but nothing else.]**
- c. Finite-horizon (terminating) simulations
 - i. Examples
 - ii. Confidence intervals for mean performance via the method of Independent Replications
- d. Initialization problems
- e. Steady-state analysis for a single system
 - i. Examples
 - ii. Confidence intervals for the steady-state mean via the method of Batch Means
 - iii. Properties of Batch Means **[The more-mathematical aspects of this topic this won't be on the test.]**
 - iv. Overlapping Batch Means

- v. Other methods

10. Comparing Systems

- a. Classical confidence interval for the mean of one normal population
- b. Classical confidence interval to compare the means of two normal systems
 - i. Variance completely unknown
 - ii. Paired-t CI
 - iii. Use in simulation scenarios
- c. Variance reduction techniques
 - i. Common random numbers
 - ii. Antithetic random numbers
 - iii. **Control variates [this won't be on the test]**
- d. Ranking and selection methods to compare means of >2 systems
 - i. Definition of problem
 - ii. Relevance to simulation
 - iii. Indifference-zone approach
 - iv. Normal means selection problem
 - Bechhofer's single-stage procedure
 - Extensions
 - v. Bernoulli parameter selection problem
 - Sobel and Huyett single-stage procedure
 - Extensions
 - vi. Multinomial cell selection problem
 - Multinomial review and motivation
 - Bechhofer, Elmaghraby, and Morse single-stage procedure
 - Extensions